

# Adaptive A/B Tests on Networks with Cluster Structures

Yang Liu

George Washington University

*[louisliu@gwu.edu](mailto:louisliu@gwu.edu)*

*Joint Work with Yifan Zhou, Ping Li and Feifang Hu*

March 6, 2022

# Background

---

- IT firms such as LinkedIn, Facebook, Tweeter, etc., conduct thousands of A/B tests per day to evaluate the performance of their product (Kohavi et al., 2013) .
- Their goal of the experiment is to detect the "**all versus nothing**" average treatment effect (ATE) that compares the subjects are all treated versus they are all assigned with the control.
- However, the subjects in the experiments are often involved in **social networks** which can complicate the estimation of the ATE.
- **Blessing!** The networks in A/B tests often have certain cluster structures which can be used to mimic the scenario that all of the subjects are assigned with the same treatment.

# Limitations

---

How to do it? (Existing work): graph-cluster randomization + Horvitz-Thompson estimator, i.e. using cluster as the unit for randomization (Ugander et al., 2013; Gui et al., 2015).

- This approach requires bounded cluster sizes.
- However, the clusters detected from many community detection algorithms may not have bounded cluster sizes. Therefore, the usage of graph-cluster randomization can be restricted.

# Limitations

---

This approach also subjects to the following two problems:

- Graph-cluster randomization may generate **severe imbalance** with respect to the **cluster-treated structures**. These structures are the cluster level measures characterizing the network features according to the node's status in its cluster.
- The value of the cluster-treated structures for one cluster may depend on both its own treatment assignment as well as the treatment assignments of its connected clusters. This poses certain **challenges for the design of A/B tests**.
- The **weights** used by the Horvitz-Thompson estimator largely depend on the randomization scheme, and can not reflect the relationship of the **between-cluster network interference**.

# Our Contribution

---

- We show that if the ATE from the **cluster perspective** is considered, then the corresponding Horvitz-Thompson estimator can partially **alleviate the restriction** on the usage of graph-cluster randomization.
- By using an illustrative example, we show that the **imbalance of the cluster-treated structures** and the **inappropriate weights** used by the Horvitz-Thompson estimator can greatly **impair** the evaluation of the ATE. (This problem may not be resolved since the clusters are not independent due to the connection through the network.)

# Our Approach

---

- Design Stage — Rerandomized-Adaptive Randomization
  - Use pairwise-sequential randomization (Qin et al., 2016) to balance the cluster-treated structures whose values does not depend on the assignments of other clusters.
  - Rerandomize the assignments and further select the one that also balance the cluster-treated structures whose values also depend on the assignments of other clusters.
- Estimation Stage— Cluster-Adaptive Estimator
  - propose new weights to adjust the nodes according to the nodes' treated status.

Thank you!

# References I

---

- Gui, H., Xu, Y., Bhasin, A., and Han, J. (2015). Network a/b testing: From sampling to estimation. In *Proceedings of the 24th International Conference on World Wide Web*, pages 399–409.
- Kohavi, R., Deng, A., Frasca, B., Walker, T., Xu, Y., and Pohlmann, N. (2013). Online controlled experiments at large scale. In *Proceedings of the 19th ACM SIGKDD international conference on Knowledge discovery and data mining*, pages 1168–1176.
- Qin, Y., Li, Y., Ma, W., and Hu, F. (2016). Pairwise sequential randomization and its properties. *arXiv preprint arXiv:1611.02802*.
- Ugander, J., Karrer, B., Backstrom, L., and Kleinberg, J. (2013). Graph cluster randomization: Network exposure to multiple universes. In *Proceedings of the 19th ACM SIGKDD international conference on Knowledge discovery and data mining*, pages 329–337.